Cryptography Engineering

- Lecture 9 (Jan 16, 2024)
- Today's notes:
 - Recall previous contents
 - The OPAQUE protocol
 - Summary on password-based authentication
 - Notes on the final project
- Coding tasks/Homework:
 - Implement the OPAQUE protocol
 - Bonus: Implement OPAQUE using sockets

Previous lecture contents

• Welcome back from the Christmas holidays!

- L1: Recall some cryptographic primitives
- L2: Signature and Certificate
- L3: DHKE + Signature & Certificate = TLS handshake
- L4: Secure Messaging, E2EE, X3DH
- L5 & L6: Key chain, Double ratchet = Symmetric ratchet + DH ratchet
- L7: Passwords, Off/Online attacks, TLS + passwords, Salting
- L8: SCRAM (hashed+salted+iterated), Password-based AKE (EKE, SRP)

- TLS + hashed & salted passwords
- The SCRAM protocol
- The EKE protocol
- The SRP protocol

- TLS + hashed & salted passwords
- The SCRAM protocol
- The EKE protocol
- The SRP protocol
- Goal: Authentication via passwords; Resistance to offline attacks.

TLS + hashed & salted passwords

- Store (r, H(pw, r)) in the server, where r is the salt.
- Transport r to the client, then the client prove its identity by responding H(pw,r)
- Encrypted by TLS
- The SCRAM protocol
- The SRP protocol

- TLS + hashed & salted passwords
- The TLS + SCRAM protocol
 - Store $(r, n, H^n(pw, r))$ in the server, where r is the salt and n is the number of iterations.
 - Transport r and n to the client, then the client prove its identity by responding $H^n(pw,r)$
 - Encrypted by TLS
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- TLS + hashed & salted passwords
- The TLS + SCRAM protocol
- The SRP protocol
 - Store (r, H(pw, r)) in the server, where r is the salt.
 - Password-based AKE:
 - Security guarantee even if the certificate is fake or the TLS connection is insecure.
 - Enhanced security via integrating with TLS

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- The TLS + SCRAM protocol
- The SRP protocol
- Advantage of storing hashed-salted passwords:
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Storage	Required Time after leakage	
Plain pw	0(1)	
H(pw)	O (<i>D</i>)	
r, H(pw, r)	O (<i>D</i>)	

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- Advantage of storing hashed-salted passwords:
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 - 2. Increase the time required to recover the password after leakage.

This is also important in practice, e.g., notifying users to change their passwords after the leakage.

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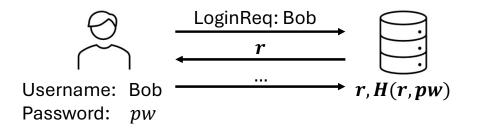
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- Advantage of storing hashed-salted passwords:
 - 1. Avoid cross-system leakage
 - 2. Increase the time **required to recover the password after leakage**.
- All protocols reveal salt (and the number of iterations) during the execution...
 - May lead to Precomputation Attacks
 - $\mathbf{O}(|\mathbf{D}|) \rightarrow \mathbf{O}(\log|\mathbf{D}|)$ or even $\mathbf{O}(1)$

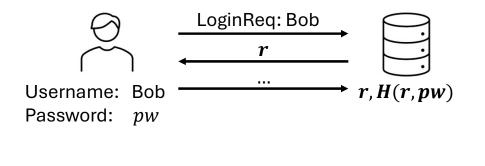
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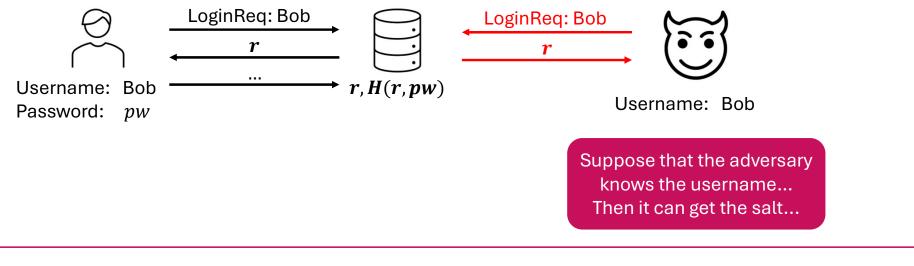


Username: Bob

Suppose that the adversary knows the username...

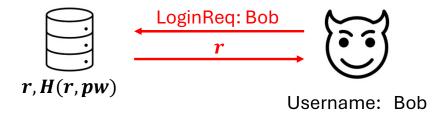
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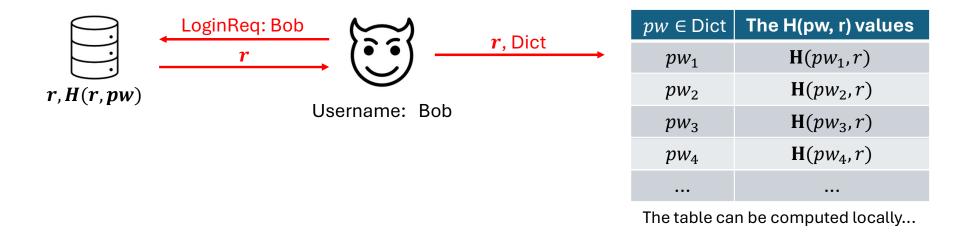


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- Suppose that the password is stored by hashing and salting.
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 - Precompute a table containing all hashed passwords with the same salt:



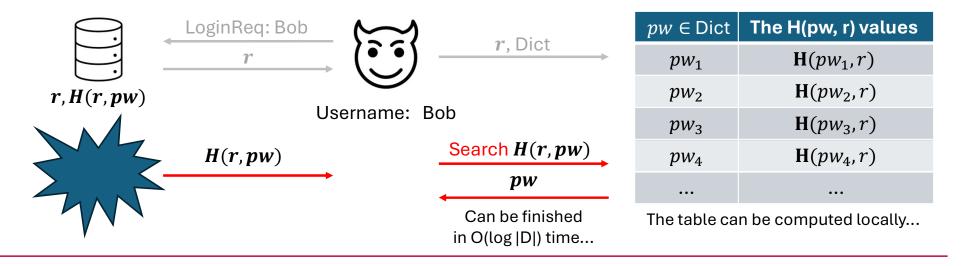
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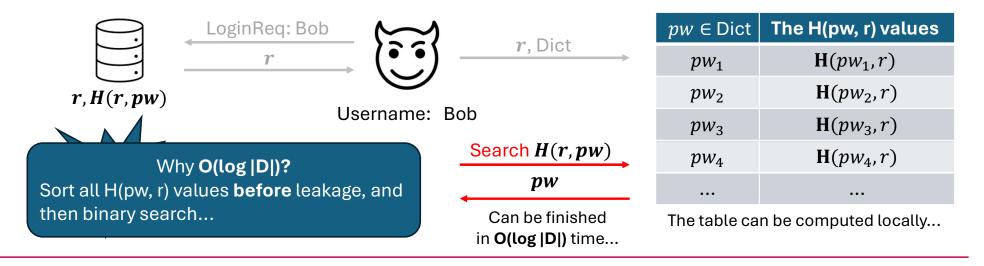
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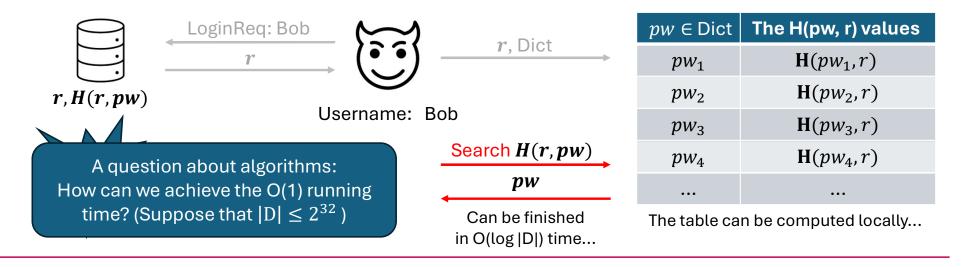
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\bigcirc	LoginReq: B		7 Dict	$pw \in Dict$	The H(pw, r) values
· · ·	r	(💽 /	r, Dict →	pw_1	$\mathbf{H}(pw_1,r)$
т Ш(т т				pw_2	$\mathbf{H}(pw_2, r)$
Storage	Required Time after leakage	with precomputation		pw_3	$\mathbf{H}(pw_3, r)$
Plain pw	0(1)	O (1)	$\mathbf{H}(r, pw)$	pw_4	$\mathbf{H}(pw_4,r)$
H(pw)	O (D)	O (log D)	pw		•••
r, H(pw, r)	O (D)	O (log D)	an be finished J(log D) time	The table ca	n be computed locally

• Comparison:

Attack Method to recover pw	Required Time <u>before</u> leakage	Required Time <u>after</u> leakage
Brute-force on Dictionary	-	O (<i>D</i>)
Precomputation	$\leq 0(\mathbf{D} \cdot \log \mathbf{D})$	$\leq 0(\log \boldsymbol{D})$

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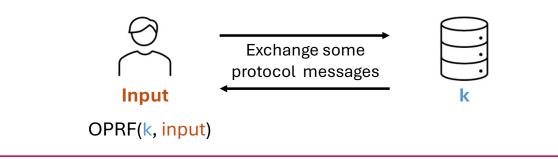
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- Reveal salt during the protocol => Precomputation attacks
- How can we protect the salt?
 - No straight-forward solutions that without using algebraic structures
 - Solution using algebraic structures: **Oblivious Pseudorandom Function** (OPRF)
- PAKE without revealing salt: **OPAQUE**

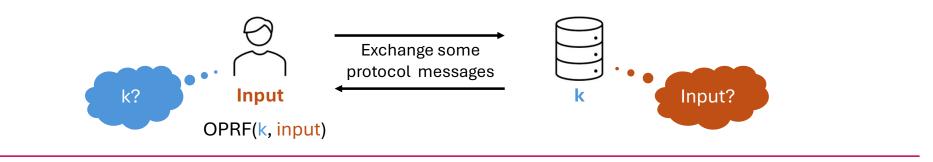
- Classical PRF:
 - Pseudorandomness: If the PRF key is random, then the output of PRF is pseudorandom

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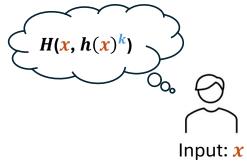
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- Classical PRF:
 - Pseudorandomness: If the PRF key is random, then the output of PRF is pseudorandom
- Oblivious PRF:
 - Pseudorandomness
 - PRF in the two-party (client-server) computation setting
 - Key privacy: The client learns OPRF(k, input), but it learns nothing about the key k
 - Input privacy: The server knows the client has evaluated the ORRF, but it does not know the input



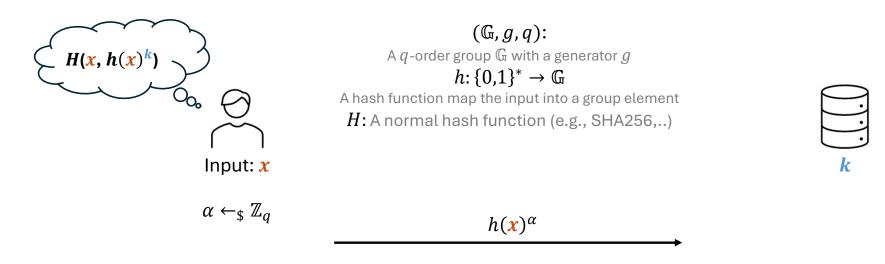
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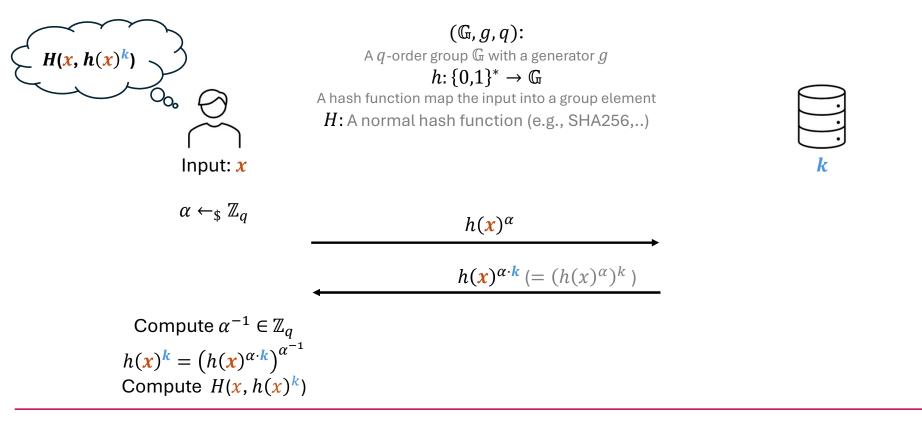


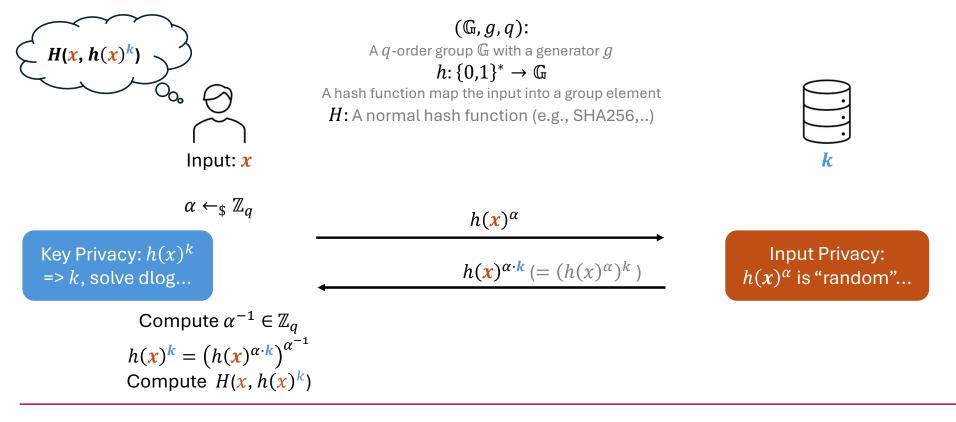
 (\mathbb{G}, g, q) : A q -order group \mathbb{G} with a generator g $h: \{0,1\}^* \to \mathbb{G}$ A hash function map the input into a group element *H*: A normal hash function (e.g., SHA256,..)

k

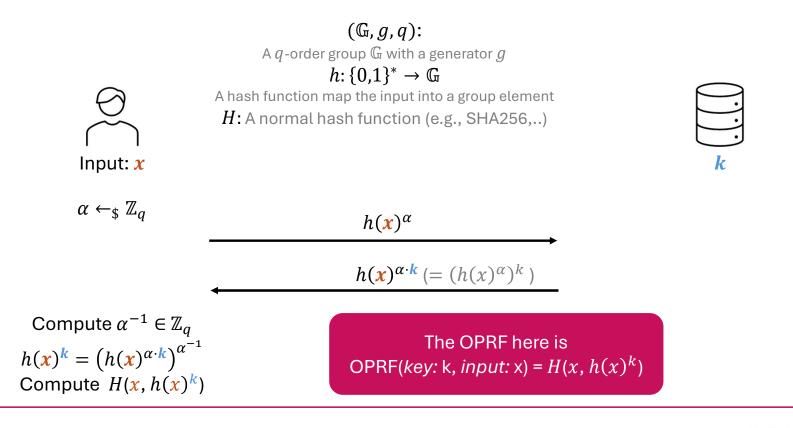
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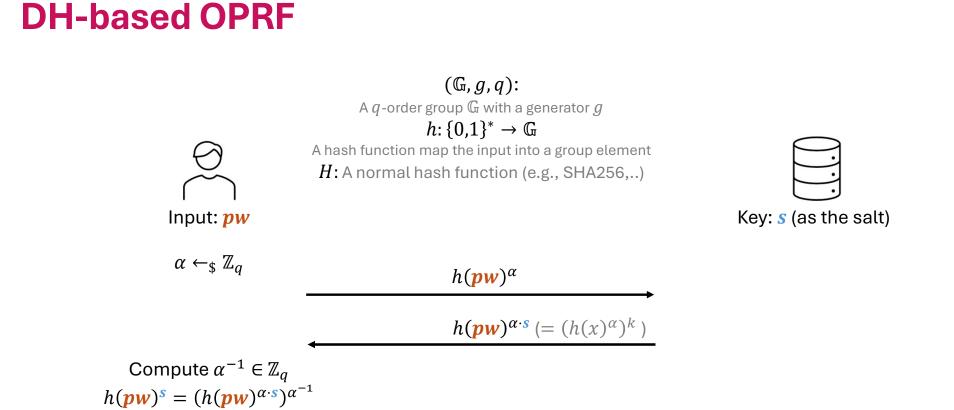






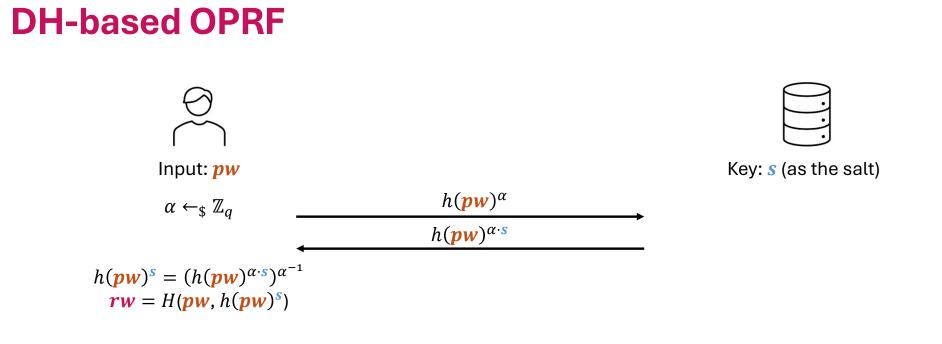






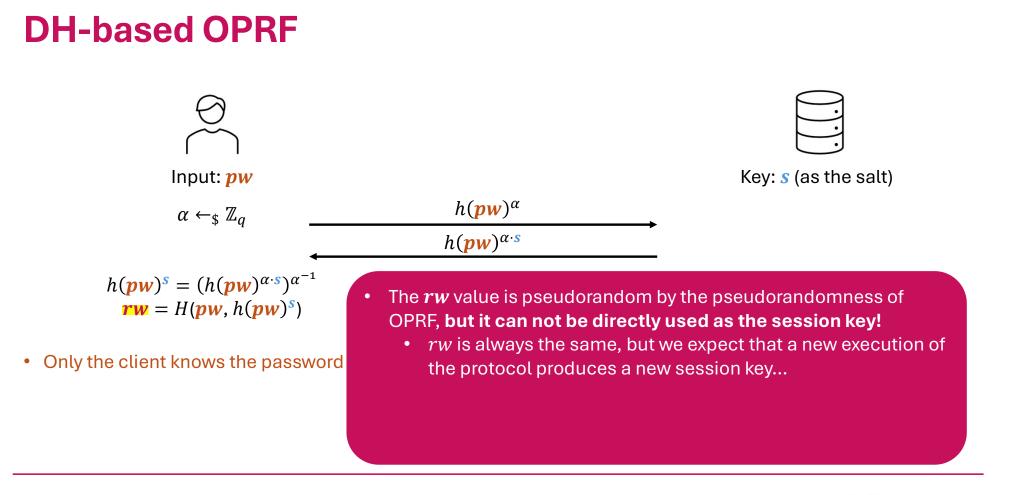
Compute $H(pw, h(pw)^s)$

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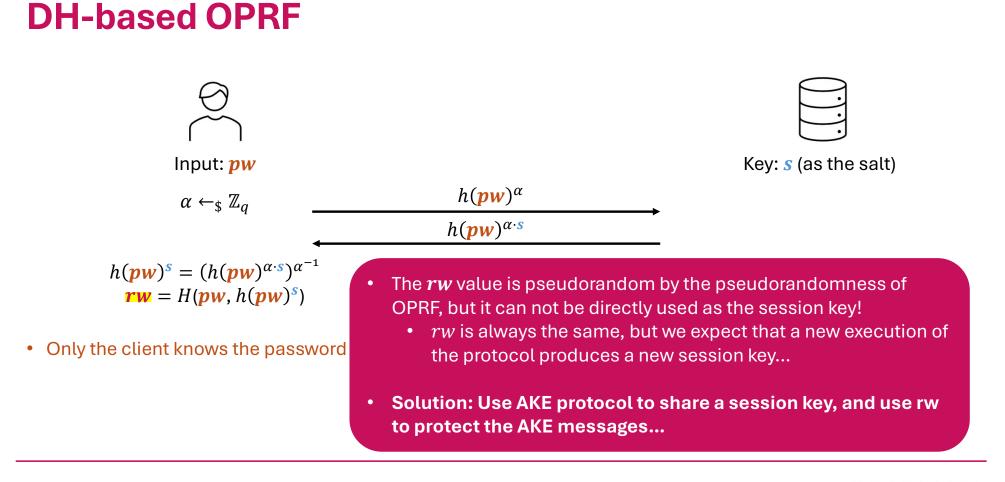


• Only the client knows the password

• Only the server knows the salt



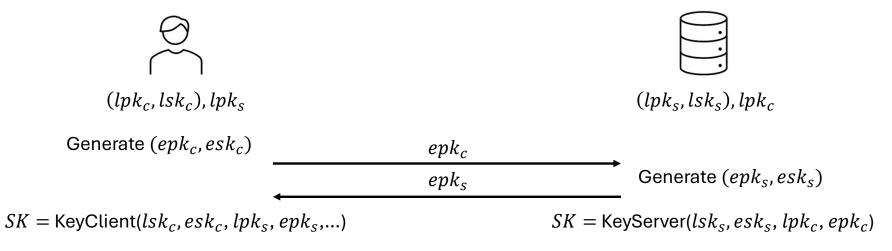
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- Brief introduction of AKE (Authenticated Key Exchange)
 - Two parties share an authenticated key using their long-term key pairs

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 - Two parties share an authenticated key using their long-term key pairs
 - For example:



• Security Requirement: Pseudorandom session key, authentication, ...



pw

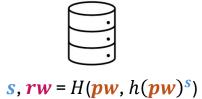


 $s, rw = H(pw, h(pw)^s)$

Suppose that the server has the rw value



pw



 $(lpk_c, lsk_c) \leftarrow AKE.KeyGen$ $(lpk_s, lsk_s) \leftarrow AKE.KeyGen$

Generate AKE key pairs



pw



 $s, rw = H(pw, h(pw)^s)$

 $(lpk_c, lsk_c) \leftarrow AKE.KeyGen$ $(lpk_s, lsk_s) \leftarrow AKE.KeyGen$

key_info = (lpk_c, lsk_c, lpk_s)

rw_key = KDF(*rw*)
enc_keys = AEAD(rw_key, key_info)

Encrypt generated keys using rw

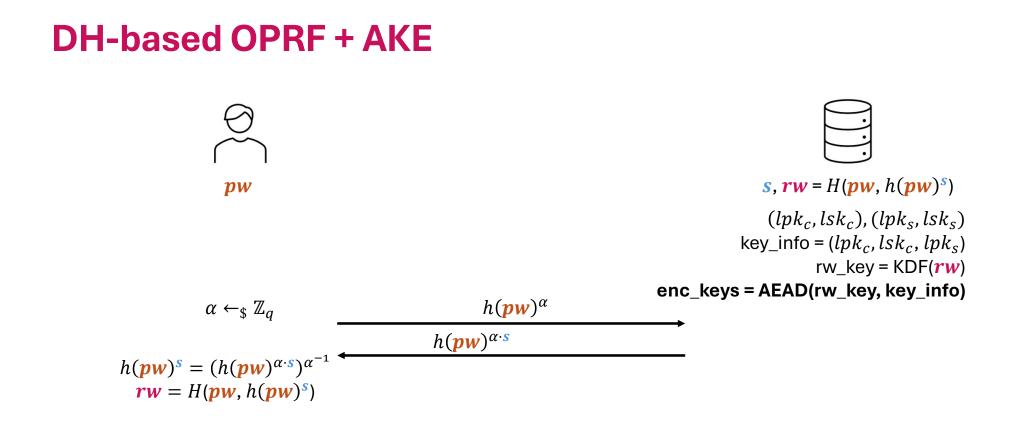


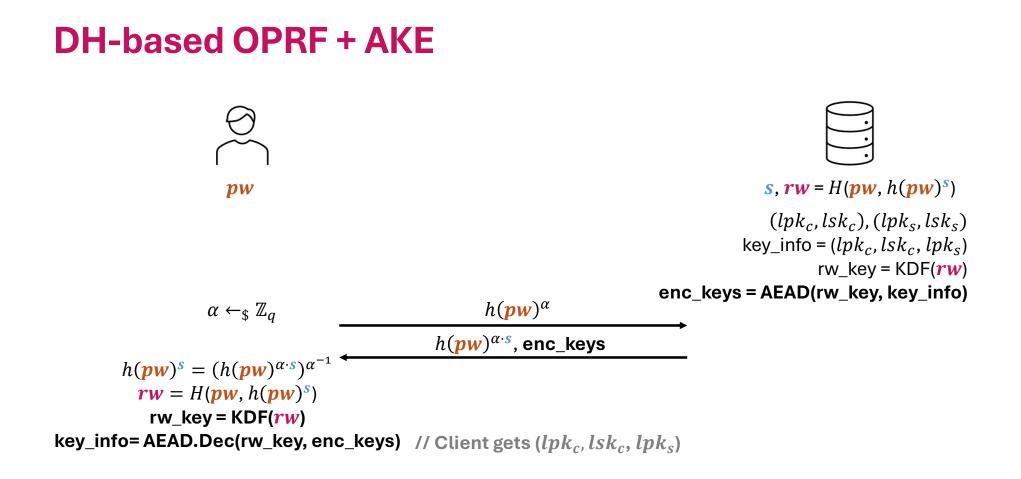
pw

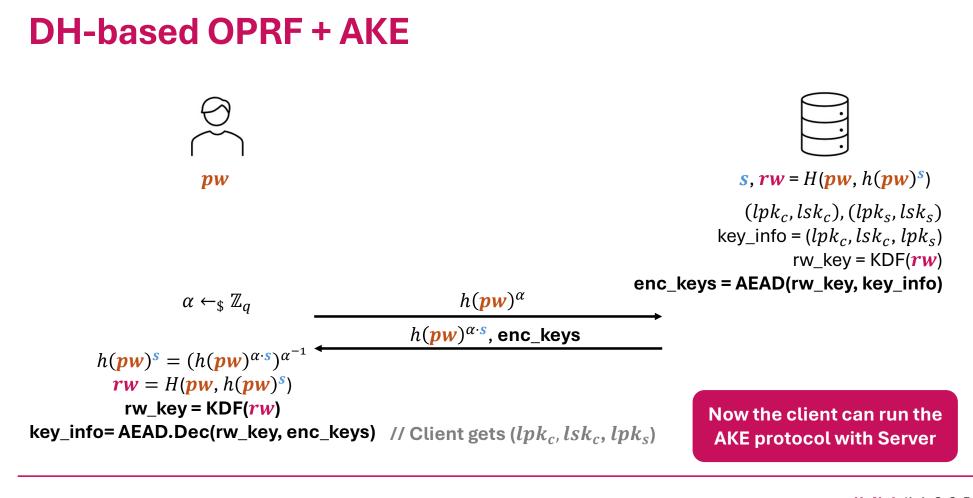


 $s, rw = H(pw, h(pw)^s)$

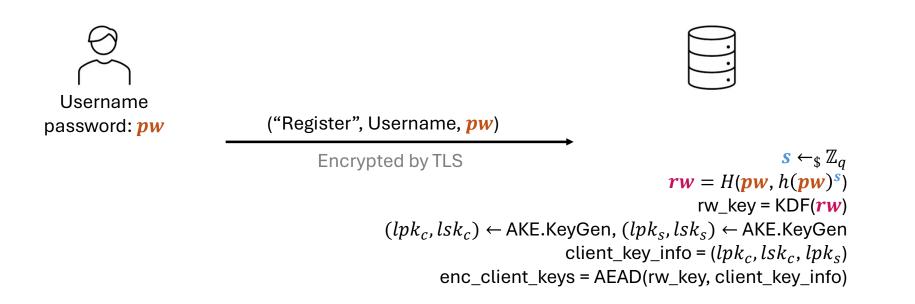
 $(lpk_c, lsk_c), (lpk_s, lsk_s)$ key_info = (lpk_c, lsk_c, lpk_s) rw_key = KDF(*rw*) enc_keys = AEAD(rw_key, key_info)



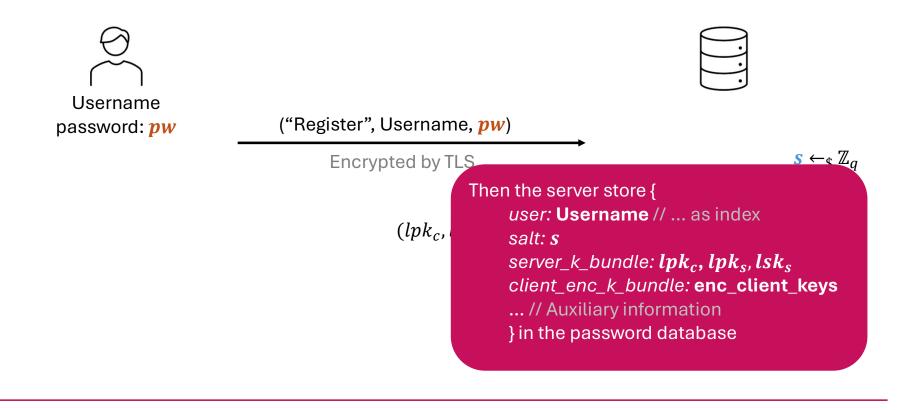




OPQAUE – Overview of Registration



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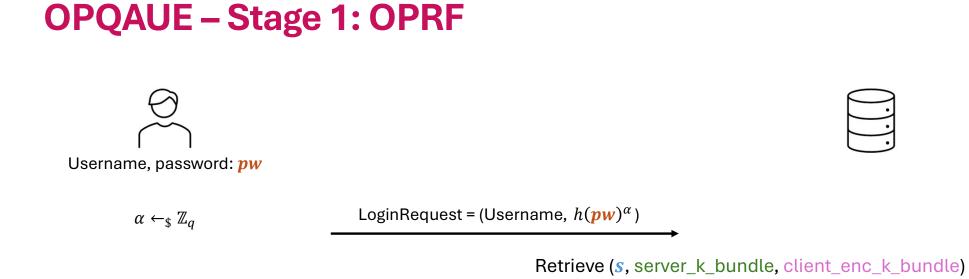
OPQAUE – Stage 1: OPRF



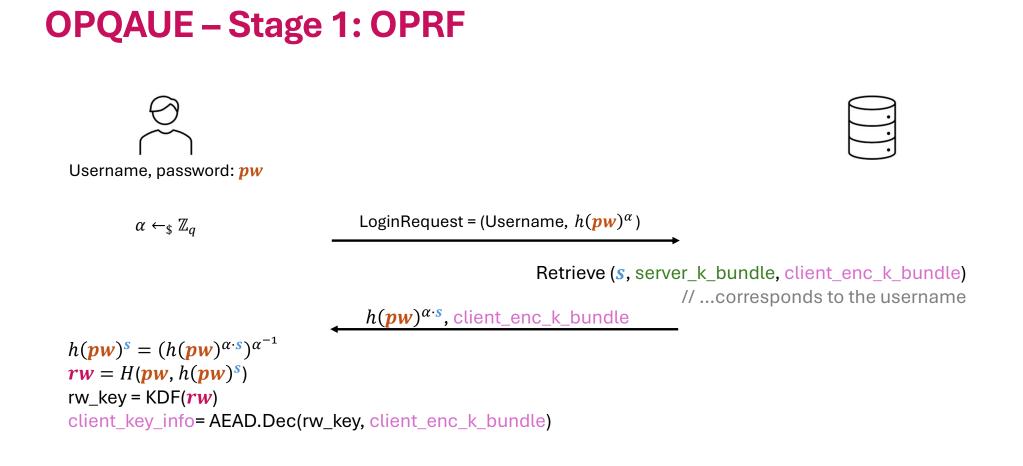


LoginRequest = (Username, $h(pw)^{\alpha}$)

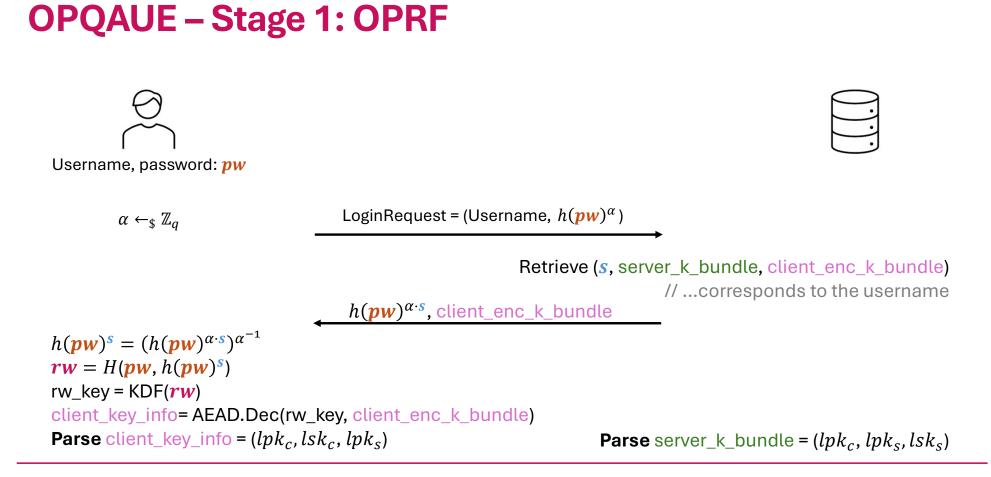


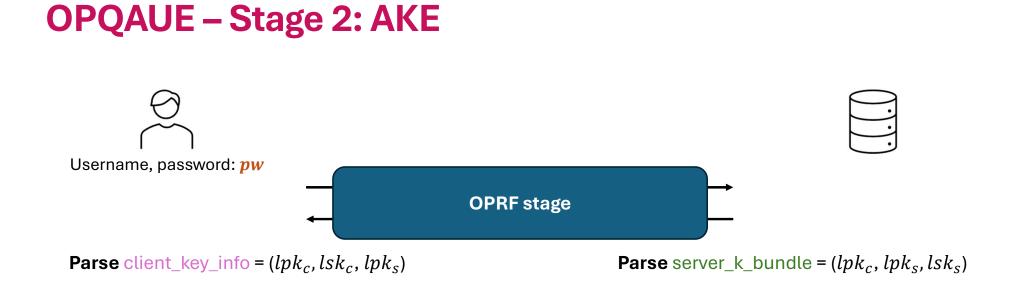


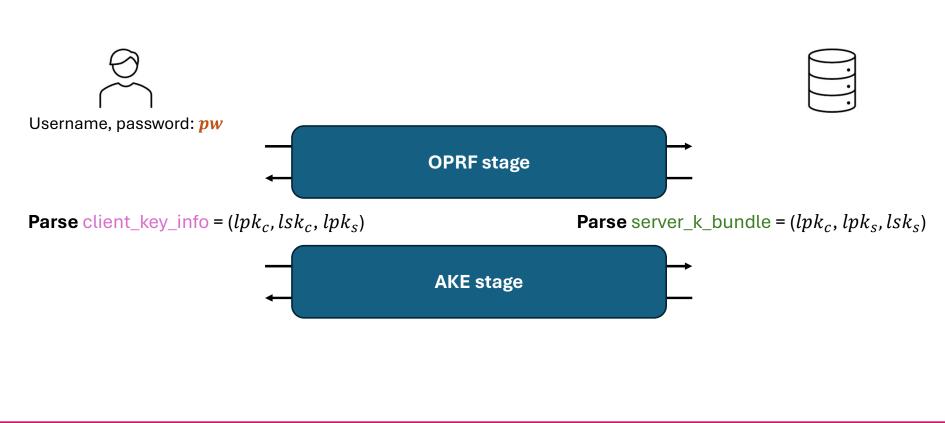
// ...corresponds to the username



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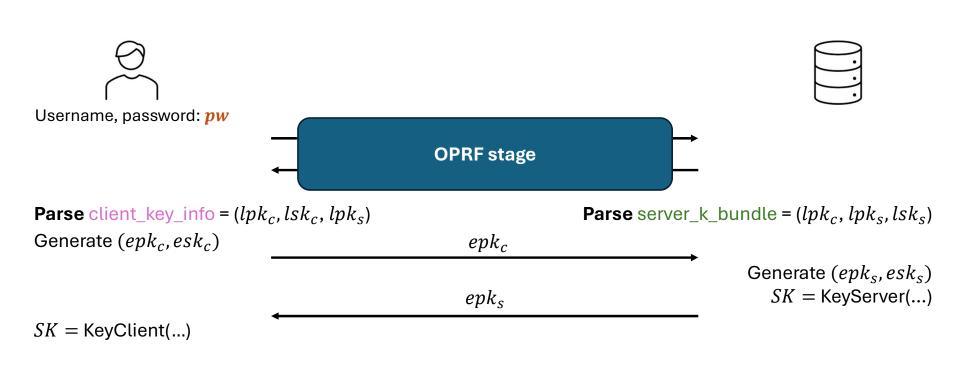




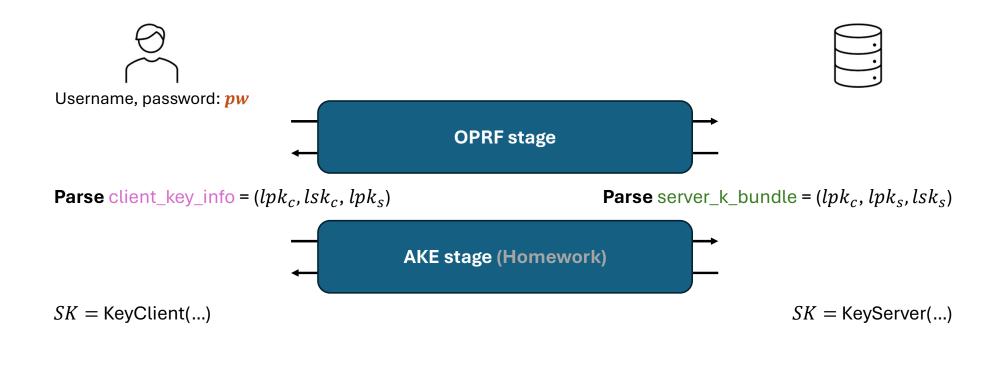


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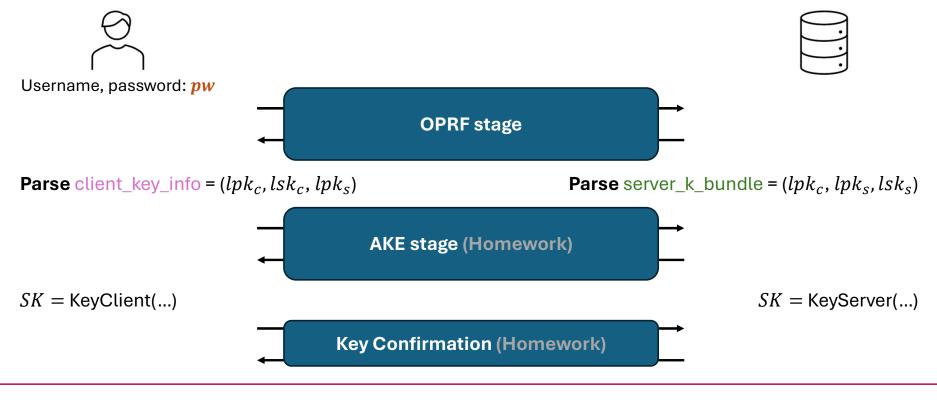
OPQAUE – Stage 2: AKE



OPQAUE – Stage 2: AKE



OPQAUE – Stage 3: Key Confirmation



OPQAUE – Stage 3: Key Confirmation

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OPQAUE – Summary

Username, password: **pw**

Registration: Instead of storing (salt, H(salt pw)), we store (salt, AEAD(rw, [AKE keys], ...)), where rw = DH-OPRF(salt, pw) // This allows the future messages exchange to not reveal the salt (to prevent precomputation)

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OPRF stage:

Allow the client to compute rw (to recover the AKE keys) without revealing the salt

AKE stage:

Use AKE protocol to share a fresh session key

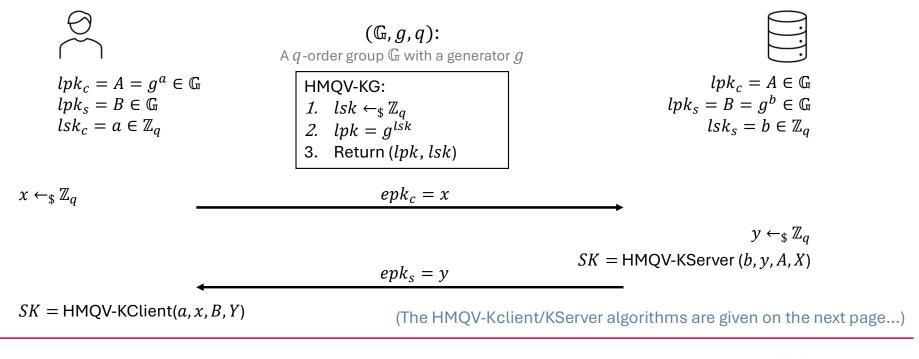
Key Confirmation:

Confirm both parties share the same key

Summary on Password-based Authentication

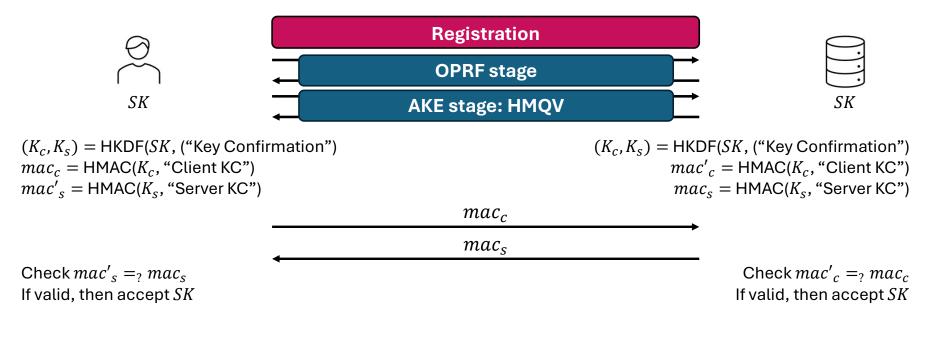
- Use passwords to authenticate identities
- Storage of passwords & Protocols:
 - Plaintext (or hashed without salt) password:
 - Hashed + salted password: 1 (SRP, ...)
 - Hashed + salted + iterated password: 1 (SCRAM, ...)
 - OPRF passwords:
- In Practice: Run over TLS
- Password-based AKE protocols: (secure guarantee even in an insecure TLS connection...)
 - SRP
 - OPAQUE (stronger)

- Implement the DH-OPRF protocol, and use it to implement the OPAQUE registration phase (using the example code).
- Implement the HMQV AKE protocol



HMQV-KClient(a, x, B, Y) 1. d = SHA256(X, [Client's Name])2. e = SHA256(Y, [Server's Name])3. $ss = (YB^e)^{x+da \setminus mod q}$ 4. SK = HKDF(ss) HMQV-KServer(b, y, A, X) 1. d = SHA256(X, [Client's Name])2. e = SHA256(Y, [Server's Name])3. $ss = (XA^d)^{y+eb \setminus mod q}$ 4. SK = HKDF(ss)

• Implement the OPAQUE protocol instantiating with the HMQV protocol, where the Key Confirmation works as follows:



- (Bonus) Implement the OPAQUE protocol (in the non-bonus homework) using sockets.
- (Bonus) What is the RTT of the OPAQUE protocol in the non-bonus homework? Can you improve it? If so, implement your improved version (can be without sockets)
 - One RTT = One " , " in the protocol...

Further Reading

- OPAQUE paper: <u>https://eprint.iacr.org/2018/163</u>
- OPAQUE IETF draft: https://www.ietf.org/archive/id/draft-irtf-cfrg-opaque-02.html
- HMQV paper: https://eprint.iacr.org/2005/176

Notes on Homework

- 1 non-bonus homework question = 1 point
- 1 *bonus* homework question = 2 points
- How to calculate the final grade of homework (≤ 40):

 $40 \times \begin{pmatrix} \text{points you obtain} \\ \end{pmatrix}$ the number of questions

// You need to get at least 40 × 60% = 24 points to qualify for the final exam.

- You can submit **bonus homework before the final deadline: Feb 7**th, 2025
 - Please ensure that your code runs correctly, as you will not have an opportunity to resubmit it.
- If your code for Homework Set 1 or 2 does not run correctly...
 - You can resubmit it by the extended deadline: January 21st, 2025.
- Some suggestions:
 - Include the sample input and its expected output in the README file to help me verify your submission.