- Lecture 1 (April 23, 2025)
- Today:
 - Admin.
 - Overview of this module

Contact Information

- Course coordinator: Prof. Jiaxin Pan
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- Office hours
 - Office: Room 2628
 - 2 pm 2:30 pm, Wednesday
 - (Please send an email in advance)
- All information is available on:
 - https://runzhizeng.github.io/QC-s25/



- Summer semester 2025: 23.04.2025 24.07.2025
- 14 Weeks: Wednesday and Thursday every week
- Lecture dates:
 - April: 23, 24, 30
 - May: 01(Labor Day), 7, 8, 14-15 (Travel), 21, 22, 28-29 (Ascension)
 - June: 4, 5, 11, 12, 18, 19(Corpus Christi), 25, 26.
 - July: 2, 3, 9, 10, 16, 17, 23, 24.

Format

- Wednesday 12:00 13:30:
 - Two lectures (~40min each) + 10min break
- Thursday 10:00 12:00:
 - One lecture (~45min)
 - Exercise and Q&A (~45min-1h)
 - Explanation of selected exercise questions (~15min-30min)
 - I may ask you to present your solutions
- This module involves a large amounts of calculations
 - Please bring your **pen and paper (especially on Thursday!)**
 - You can also bring your laptop/iPad to check the lecture notes at any time

Resources

- Lecture notes: Will be updated at https://runzhizeng.github.io/QC-s25
- Calculation Manuscripts: Would be updated at the Moodle.
- Textbooks:
 - Quantum Computation and Quantum Information by Michael Nielsen and Isaac Chuang
 - Linear Algebra and Learning from Data by Gilbert Strang
 - An Introduction to Quantum Computing by Phillip Kaye, Raymond Laflamme, and Michele Mosca.
 - Quantum Computing: A Gentle Introduction by Eleanor Rieffel and Wolfgang Polak
 - ...

Resources

• Resources of other QC courses:

(Parts of this module are based on these external course materials)

- <u>Quantum Computation and Information</u> (Videos) by Prof. Ryan O'Donnell (Carnegie Mellon University)
- <u>Quantum Cryptography</u> by Prof. Qipeng Liu (UC San Diego)
- <u>Quantum Cryptography</u> by Prof. Mark Zhandry (Princeton University)
- Introduction to Quantum Computing by Prof. Dakshita Khurana and Prof. Makrand Sinha (University of Illinois)
- Introduction to Quantum Computing by Prof. Henry Yuen (Columbia University)
- <u>Lecture Notes of Quantum Information Science</u> by Prof. Scott Aaronson (UT Austin)
- Miscellaneous:
 - <u>Qubit Zoo</u>: "Zoo" of interesting qubits and quantum gates
 - Quantum Programming (Simulated): <u>Q#</u> and <u>Qiskit</u>

Homework and Exam

- Homework: Some problem sets (notice time: 1~2 weeks).
- Exam type (Oral or written?): To be decided
- When? To be decided

What is Quantum Computing?

- Computation based on **quantum mechanics**, rather than classical physics
- Quantum mechanics:
 - Classical physics does not work in some cases
 - -> Quantization, introduced/explained by Planck, Einstein, ...
 - -> Quantum theory, formalized by Schrödinger, Heisenberg, Dirac...

- Computation based on **quantum mechanics**, rather than classical physics
- Quantum mechanics:
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Classical physics:

- "Light is continuous wave (with energy)
- \Rightarrow Shine light on the plate for a long time
- \Rightarrow Electrons should be emitted eventually"





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Double slit experiment: Light is a wave, or at least it behaves like a wave https://en.wikipedia.org/wiki/Double-slit_experiment

Example: Photoelectric effect



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Reality (Experiments):

1. There is a *threshold frequency*.

(Electrons are emitted **only if** the light's frequency is high enough)

2. The emission of electrons is "immediately", regardless of light's intensity

Example: Photoelectric effect



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Computation based on **quantum mechanics**, rather than classical physics ٠

be emitted eventually"

- Quantum mechanics: ۲
 - Classical physics does not work in some cases •



(Source: Wikipedia)(Electrons are emittee 2. The emission of electro

Wenn sich nämlich bei der Ausbreitung eines Lichtstrahls die Energie nicht kontinuierlich im ganzen Raum verteilt, sondern aus einzelnen, im Raum lokalisierten Quanten besteht, dann erklärt das diemerkwürdigen Eigenschaften der Photoelektrizität...



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 - -> Quantization, introduced/explained by Planck, Einstein, ...

Example: $E = h \cdot v$ *E*: Energy of the photon

- *h*: Planck's constant
- *v*: Frequency of the photon



(Source: Wikipedia)



Example: Photoelectric effect

- Computation based on **quantum mechanics**, rather than classical physics
- Quantum mechanics:
 - Classical physics does not work in some cases
 - -> Quantization, introduced/explained by Planck, Einstein, ...
 - -> Quantum theory, formalized by Schrödinger, Heisenberg, **Dirac**, ...



 $i\hbar \frac{d}{dt} |\Psi(t)\rangle = \widehat{H}(\Psi(t))$

(Schrödinger equation)

(Source: Wikipedia)



Schrödinger's Cat (picture from Medium)



 $egin{aligned} U|\psi
angle &=\langle \phi|\psi
angle U|\psi
angle \ (Dirac's notation) \end{aligned}$

(Source: Wikipedia)



(Heisenberg Uncertainty Principle) (Source: Wikipedia)



• Computation based on **quantum mechanics**, rather than classical physics

Quantum Mechanics Information Theory + Quantum Mechanics = Quantum Computing



...

(Source of pictures: Wikipedia)

- Computation based on quantum mechanics, rather than classical physics
 - Quantum Mechanics
- Information Theory + Quantum Mechanics = Quantum Computing



Richard Feynman

- Simulating quantum systems with classical computers is *inefficient*
- Quantum Systems/Computers are required



...

(Source of pictures: Wikipedia)



David Deutsch

- Deutsch's algorithm, Deutsch-Jozsa algorithm
- Quantum Turing Machine

• Computation based on **quantum mechanics**, rather than classical physics

Quantum Mechanics Information Theory + Quantum Mechanics = Quantum Computing



...

(Source of pictures: Wikipedia)





Peter Williston Shor

- Breakthrough: Shor's algorithm
- Break most of existing public-key cryptosystems
- ... which motivates "post-quantum cryptography"

Lov K. Grover

- Grover search: A Quantum search algorithm
- Significant impacts on information theory, computational complexity, cryptography, ...

• Computation based on quantum mechanics, rather than classical physics

Quantum Mechanics

Information Theory + Quantum Mechanics = Quantum Computing



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D:Wave

Advances in quantum

computing



(Source of pictures: Wikipedia)

• Computation based on **quantum mechanics**, rather than classical physics

Quantum Mechanics

Information Theory + Quantum Mechanics = Quantum Computing







Advances in quantum



We are now in the NISQ era!

NISQ = Noisy Intermediate-Scale Quantum

- Not yet powerful enough to run Shor's or Grover's algorithms at scale
- But quantum hardware is **scaling up!**
- Quantum error correction is still needed for fault-tolerant computing

(Source of pictures: Wikipedia)

(Classical World) (Quantum World)



• **0** = Low voltage (e.g., 0V)

• **1** = High voltage (e.g., 3.3V – 5V)



(Classical World) (Quantum World)

(Source of pictures: Wikipedia)



(Source of pictures: Wikipedia)





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(11 million light-years) Taking effect needs at least 11 million years! (Maximum speed: Speed of light)



(Classical World) (Quantum World)



(11 million light-years) Taking effect needs at least 11 million years! (Maximum speed: Speed of light)



(Classical World) (Quantum World)



- What makes Quantum Computing powerful?
 - Quantum Superposition Qubits
 - Unitary quantum gates instead of logic gates
 - Quantum Entanglement
 - Quantum Measurement
 - Quantum algorithms utilizing quantum properties...

Impact on Computational Complexity

- Exponential speedups for some specific problems
 - Factoring, discrete logarithm, or more generally, hidden (finite abelian) subgroup problem

• Polynomial speedups for generic search problems

- Grover search
- Improve some lower bounds

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Quantum Computers ≠ More "Computable"

• They cannot solve uncomputable problems (e.g., the halting problem)

Quantum Computers ≠ Always more efficient

• No known advantage in many problems (e.g., Traveling Salesman Problem)

Overall Goals

- Main topics:
 - Quantum mechanics and its linear algebra formulation
 - Entanglement and Measurement
 - Quantum Algorithms:
 - Described by quantum gates/circuits, unitaries
 - Quantum "parallelism" evaluation on superposition
 - Applications of quantum algorithms QKD, QFT, search, ...
 - Quantum Information
 - Quantum Programming (TBD)?

Overall Goals

- After completing this module, you should be able to:
 - Explain the fundamental principles of quantum computing (QC) and basic quantum mechanics.
 - **Use** the relevant linear algebra (including qubit representations and quantum gates) to formalize quantum computing notions and perform **basic calculations**.
 - **Describe and apply** quantum algorithms such as the Quantum Fourier Transform and Grover's search algorithm.
 - **Design** some simple quantum circuits/algorithms based on the algorithms you learned
 - **Read and understand** introductory research papers on quantum computing and cryptography.

We do not know where • is... Or, • is in "superposition"...

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Measurement

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Measurement

Measurement

The state of the $|\psi\rangle = |\phi_1\rangle \otimes |\phi_2\rangle \otimes |\phi_3\rangle \otimes \cdots \otimes |\phi_n\rangle$, \otimes : Tensor product composite system:

Examples: $|0\rangle \otimes |1\rangle \otimes |1\rangle \otimes |1\rangle = |0111\rangle, |1\rangle \otimes |0\rangle \otimes |1\rangle \otimes |0\rangle \otimes |1\rangle = |10101\rangle$ $|0\rangle \otimes |1\rangle \otimes (\alpha |0\rangle + \beta |1\rangle) \otimes |1\rangle, |0\rangle \otimes |1\rangle \otimes \frac{|0\rangle + |1\rangle}{\sqrt{2}} \otimes |1\rangle$

Entanglement

 $|\psi\rangle = |\phi_1\rangle \otimes |\phi_2\rangle$

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Entanglement

Entanglement

b

Let $f: \{0,1\} \rightarrow \{0,1\}$ be a classical bit function:

The "quantum version" of f:

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Quantum Gates and Algorithms

Quantum Information – Entropy and Randomness

Quantum Information - Distinguishability

Thursday's Topic

• Quantum state, qubit, and their linear algebra formulation

• Bring your **pen** and **paper**